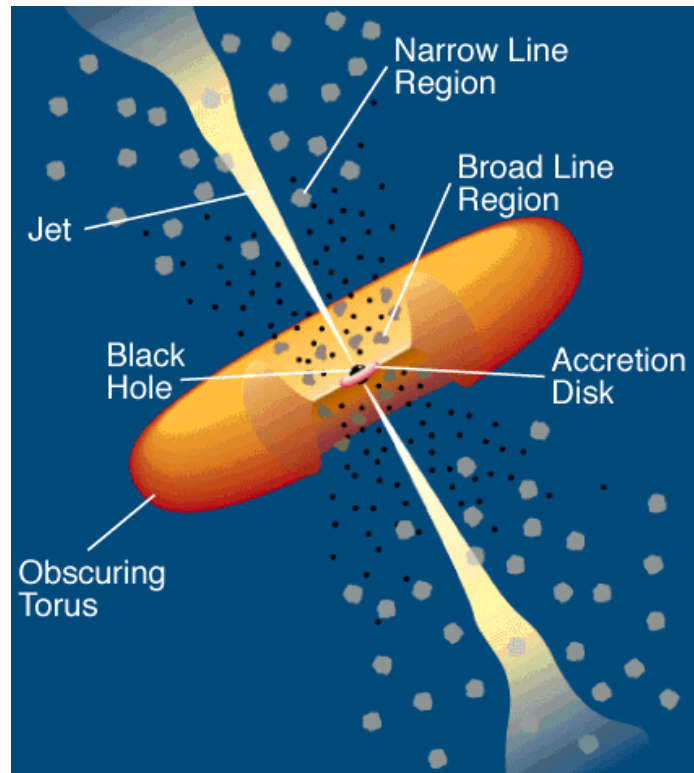


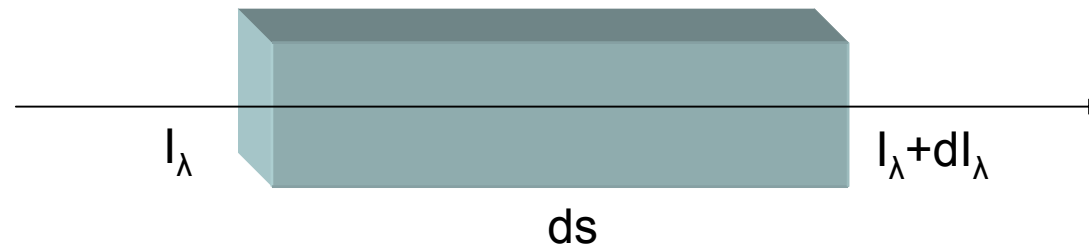
Reprocessing AGN radiation by Dust



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Absorption coefficient and optical depth

- Consider radiation shining through a layer of material. The intensity of light is found experimentally to decrease by an amount dI_λ where $dI_\lambda = -\alpha_\lambda I_\lambda ds$. Here, ds is a length and α_λ is the **absorption coefficient** [cm^{-1}]. The photon mean free path, l , is inversely proportional to α_λ .



- Two physical processes contribute to light attenuation: (i) **absorption** where the photons are destroyed and the energy gets thermalized and (ii) **scattering** where the photon is shifted in direction and removed from the solid angle under consideration.
- The radiation sees a combination of α_λ and ds over some path length L , given by a dimensional quantity, the **optical depth**:

$$\tau_\lambda = \int_0^L a_\lambda ds$$

Importance of optical depth

We can write the change in intensity over a path length as $dI_\lambda = -I_\lambda d\tau_\lambda$.
This can be directly integrated and give the extinction law:

$$I_\lambda(\tau_\lambda) = I_\lambda(0)e^{-\tau_\lambda}$$

- An optical depth of $\tau_\lambda = 0$ corresponds to no reduction in intensity.
- An optical depth of $\tau_\lambda = 1$ corresponds to a reduction in intensity by a factor of $e=2.7$.
This defines the “optically thin” – “optically thick” limit.
- For large optical depths $\tau_\lambda \gg 1$ negligible intensity reaches the observer.

Emission coefficient and source function

- We can also treat emission processes in the same way as absorption by defining an **emission coefficient**, ϵ_λ [erg/s/cm³/str/cm] :

$$dI_\lambda = \epsilon_\lambda ds$$

- Physical processes that contribute to ϵ_λ are (i) real emission – the creation of photons and (ii) scattering of photons to the direction being considered.
- The ratio of emission to absorption is called the **source function**.

$$S_\lambda = \epsilon_\lambda / \alpha_\lambda$$

Radiative Transfer Equation

- We can now incorporate the effects of emission and absorption into a single equation giving the variation of the intensity along the line of sight. The combined expression is:

$$dI_{\lambda} = -\alpha_{\lambda} I_{\lambda} ds + \varepsilon_{\lambda} ds$$

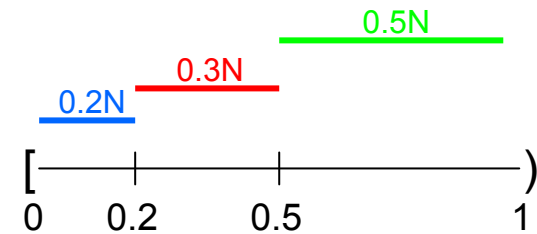
or, in terms of the **optical depth** and the **source function** the equation becomes:

$$\frac{dI_{\lambda}}{d\tau_{\lambda}} = -I_{\lambda} + S_{\lambda}$$

- Once α_{λ} and ε_{λ} are known it is relatively easy to solve the radiative transfer equation. When scattering though is present, solution of the radiative transfer equation is more difficult.

Monte Carlo – The method

- Process with 3 outcomes: Outcome A with probability 0.2
Outcome B with probability 0.3
Outcome C with probability 0.5



We select a **large** number N of **random numbers** r uniformly distributed in the interval $[0, 1)$. Approximately, $0.2N$ will fall in the interval $[0, 0.2)$, $0.3N$ in the interval $[0.2, 0.5)$ and $0.5N$ in the interval $[0.5, 1)$. **The value of a random number r uniquely determines one of the three outcomes.**

- More generally:

If E_1, E_2, \dots, E_n are n independent events with probabilities p_1, p_2, \dots, p_n and $p_1 + p_2 + \dots + p_n = 1$ then a random number r with

$$p_1 + p_2 + \dots + p_{i-1} \leq r < p_1 + p_2 + \dots + p_i$$

determines event E_i

- For continuous distributions:

If $p(x)dx$ is the probability for event $x(a \leq x < b)$ to occur then

$$\int_a^x p(\xi)d\xi = r$$

determines event X uniquely.

Monte Carlo – Procedure

Step 1: Consider a photon that was emitted at position (x_0, y_0, z_0) .

Step 2: To select a random direction (θ, φ) , pick a random number r and set $\varphi=2\pi r$ and another random number r and set $\cos\theta=2r-1$.

Step 3: To find a step s that a photon makes before an event (scattering or absorption) occurs, pick a random number r and use the probability density

$$p(\xi) = (1/l)e^{-\xi/l} \quad \text{where } l \text{ is the mean free path of the medium}$$

in equation $\int_a^s p(\xi)d\xi = r$

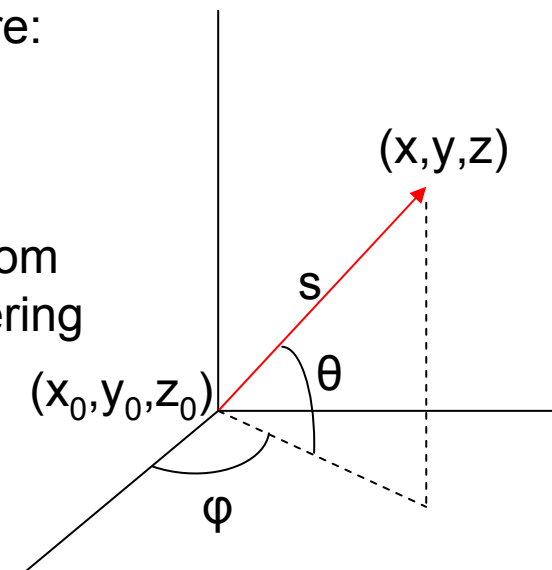
Step 4: The position of the event in space is at (x, y, z) , where:

$$x = x_0 + s \sin\theta \cos\varphi$$

$$y = y_0 + s \sin\theta \sin\varphi$$

$$z = z_0 + s \cos\theta$$

Step 5: To determine the kind of event occurred, pick a random number r . If $r < \omega$ (the albedo) the event was a scattering (go to Step 6), else, it was an absorption (record the energy absorbed and go to Step 1).



Monte Carlo – Procedure

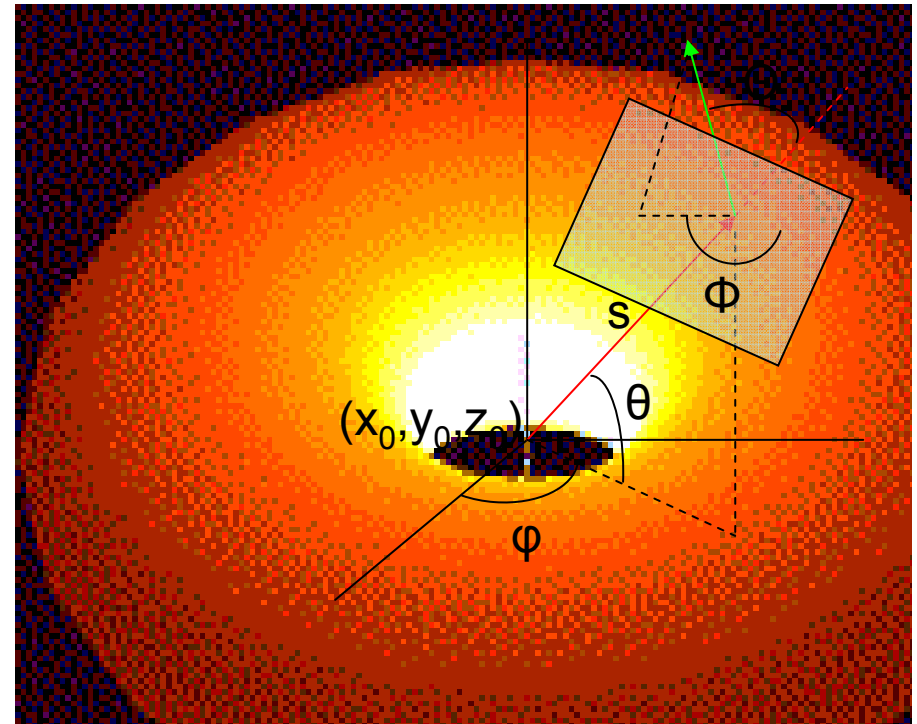
Step 6: Determine the new direction (Θ, Φ) , where Θ is the angle between the old and the new direction (to be determined from the Henyey-Greenstein phase function *) and $\Phi=2\pi r$.

Step 7: Convert (Θ, Φ) into (θ, φ) and go to Step 3.

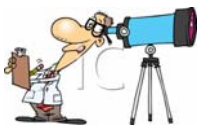
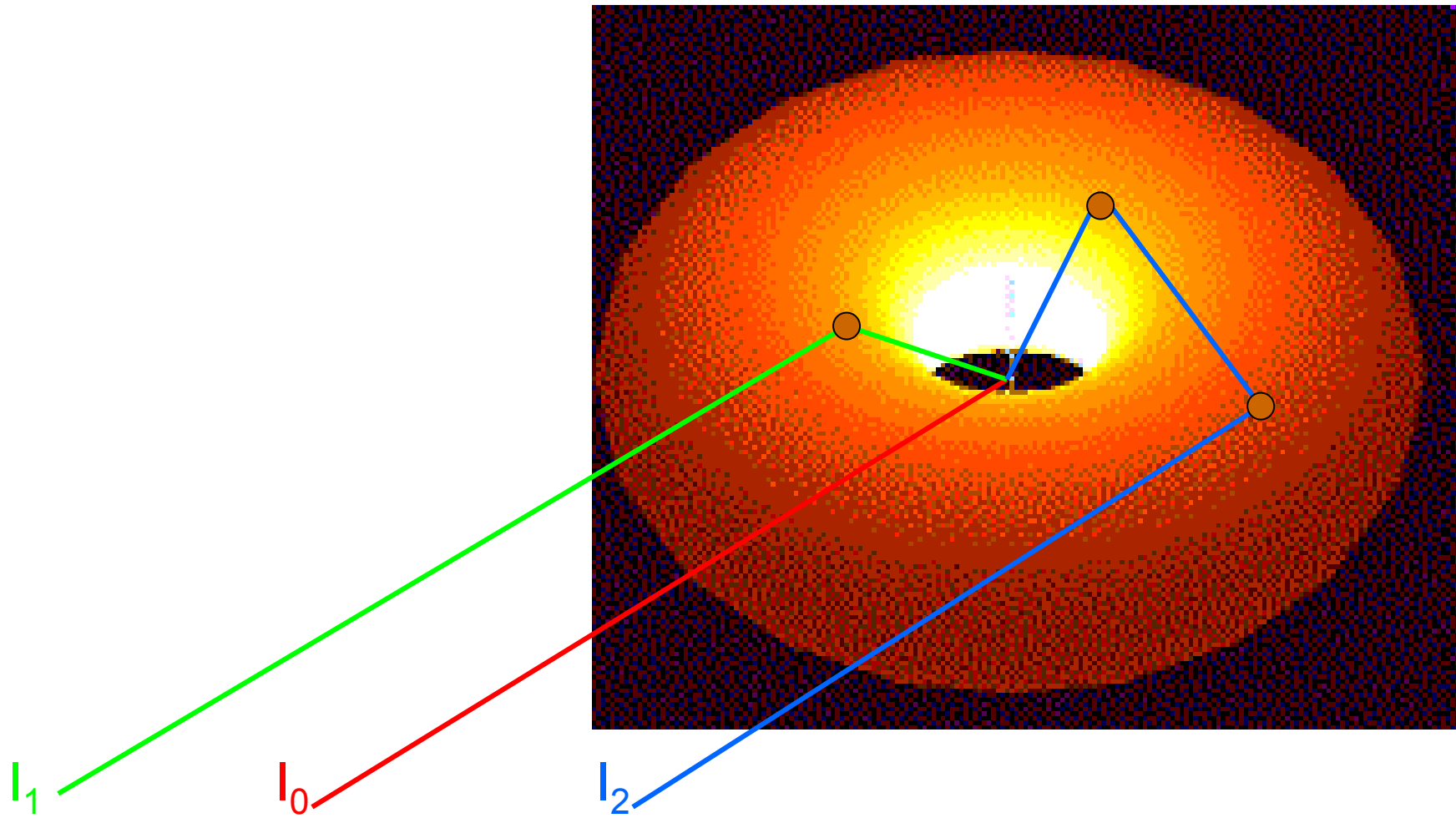
Continue the loop described above until the photon is either absorbed or escapes from the absorbing medium.

$$* p(\hat{n}', \hat{n}) = \frac{1 - g^2}{(1 + g^2 - 2g\hat{n}' \cdot \hat{n})^{3/2}}$$

Henyey & Greenstein, 1941, ApJ, **93**, 70



Scattered intensities - The method



$$I = I_0 + I_1 + I_2 + \dots$$

Scattered intensities The method

$$I = I_0 + I_1 + I_2 + \dots$$

$$I_0 = \sum_{\text{all } \Delta s} \eta(s) \Delta s e^{-\tau(s)}$$

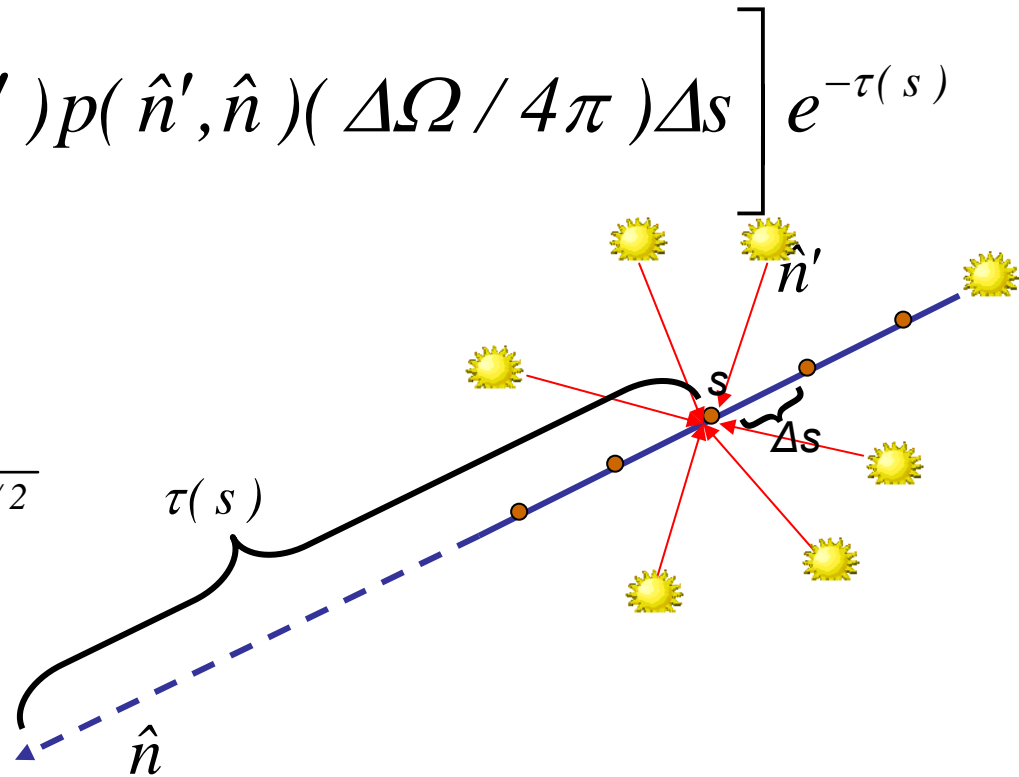
$$I_1 = \omega \sum_{\text{all } \Delta s} \left[\kappa(s) \sum_{\text{all } \hat{n}} I_0(\hat{n}') p(\hat{n}', \hat{n}) (\Delta\Omega / 4\pi) \Delta s \right] e^{-\tau(s)}$$

$$p(\hat{n}', \hat{n}) = \frac{1 - g^2}{(1 + g^2 - 2g\hat{n}' \cdot \hat{n})^{3/2}}$$

Heney & Greenstein, 1941, ApJ, 93, 70

$$\omega_V \approx 0.6$$

$$g_V \approx 0.5$$



Weingartner & Draine, 2001, ApJ, 548, 296

Scattered Intensities - Approximation

$$I = I_0 + I_1 + I_2 + \dots = I_0 \left(1 + \frac{I_1}{I_0} + \frac{I_2}{I_0} + \dots \right) = I_0 \left(1 + \frac{I_1}{I_0} + \frac{I_1}{I_0} \frac{I_2}{I_1} + \dots \right) \stackrel{\substack{I_n \approx \frac{I_1}{I_0} \\ I_{n-1} \approx \frac{I_1}{I_0} \\ n \geq 2}}{=} I_0 \left(1 + \frac{I_1}{I_0} + \left(\frac{I_1}{I_0} \right)^2 + \dots \right) =$$

$$I_0 \left(\frac{1}{1 - I_1/I_0} \right)$$

Kylafis & Bahcall, 1987, ApJ, 317, 637

Verification

1. The scattering is essentially forward

$$p(\hat{n}', \hat{n}) = \frac{1 - g^2}{(1 + g^2 - 2g\hat{n}' \cdot \hat{n})^{3/2}}$$

Heney & Greenstein, 1941, ApJ, 93, 70

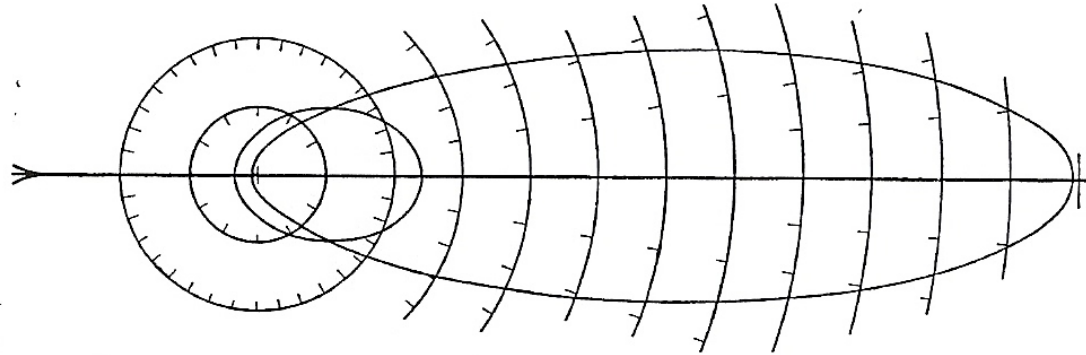


FIG. 3.—Polar diagram of the phase function of equation (2), for $\gamma = 1$. The more elongated curve is for $g = +\frac{2}{3}$; the other, for $g = +\frac{1}{3}$. The radiation is incident on the particle from the left, as shown by the arrow.

Approximation

$$I = I_0 + I_1 + I_2 + \dots = I_0 \left(1 + \frac{I_1}{I_0} + \frac{I_2}{I_0} + \dots \right) = I_0 \left(1 + \frac{I_1}{I_0} + \frac{I_1}{I_0} \frac{I_2}{I_1} + \dots \right) \stackrel{\substack{I_n \approx I_1 \\ I_{n-1} \approx I_0 \\ n \geq 2}}{=} I_0 \left(1 + \frac{I_1}{I_0} + \left(\frac{I_1}{I_0} \right)^2 + \dots \right) =$$

$$I_0 \left(\frac{1}{1 - I_1/I_0} \right)$$

Kylafis & Bahcall, 1987, ApJ, 317, 637

Verification

2. Computation of the I_2 term

$$\tau^e(V) = 100$$

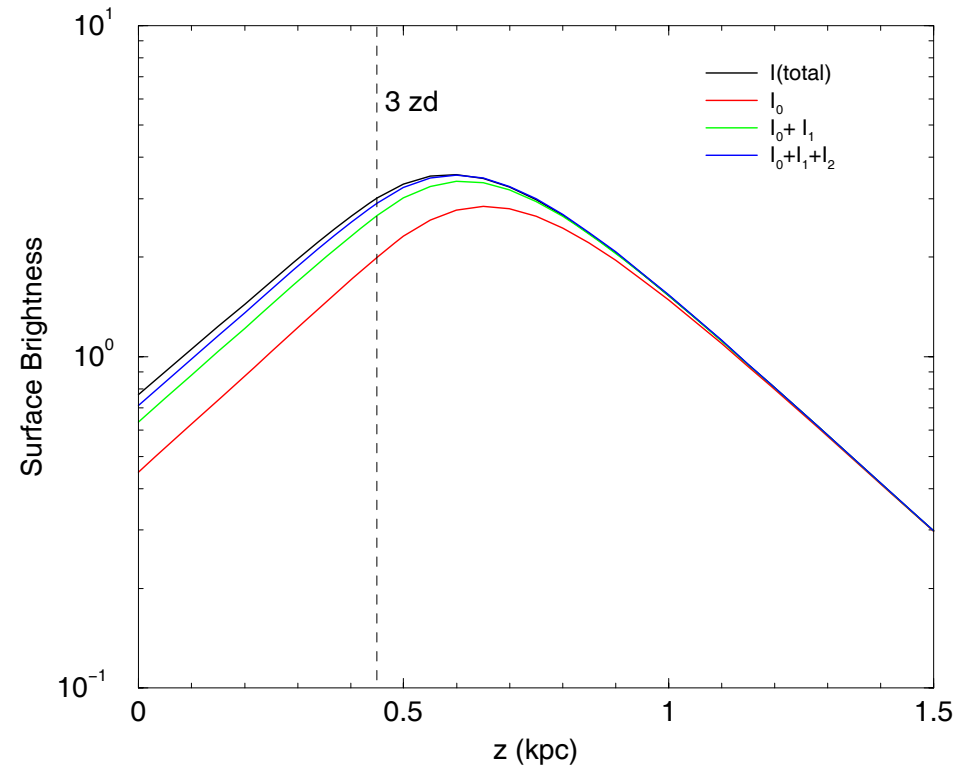
$$\theta = 90^\circ$$

$$h_s = 3 \text{ kpc}$$

$$h_d = 3 \text{ kpc}$$

$$z_s = 0.3 \text{ kpc}$$

$$z_d = 0.15 \text{ kpc}$$



Approximation

$$I = I_0 + I_1 + I_2 + \dots = I_0 \left(1 + \frac{I_1}{I_0} + \frac{I_2}{I_0} + \dots \right) = I_0 \left(1 + \frac{I_1}{I_0} + \frac{I_1}{I_0} \frac{I_2}{I_1} + \dots \right) \stackrel{\substack{I_n \approx I_1 \\ I_{n-1} \approx I_0 \\ n \geq 2}}{=} I_0 \left(1 + \frac{I_1}{I_0} + \left(\frac{I_1}{I_0} \right)^2 + \dots \right) =$$

$$I_0 \left(\frac{1}{1 - I_1/I_0} \right)$$

Kylafis & Bahcall, 1987, ApJ, 317, 637

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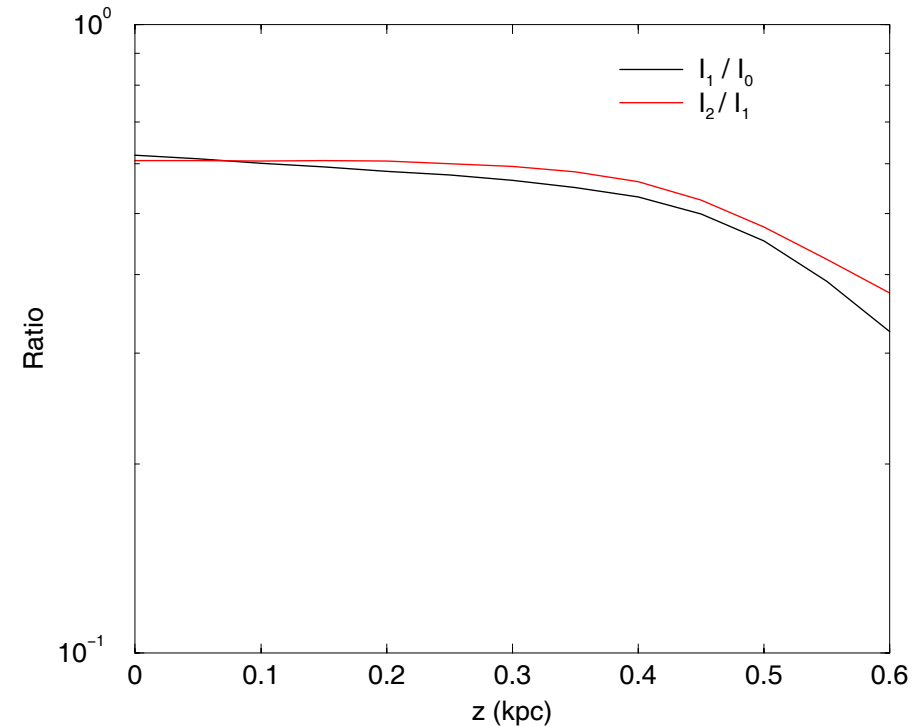
$$\theta = 90^\circ$$

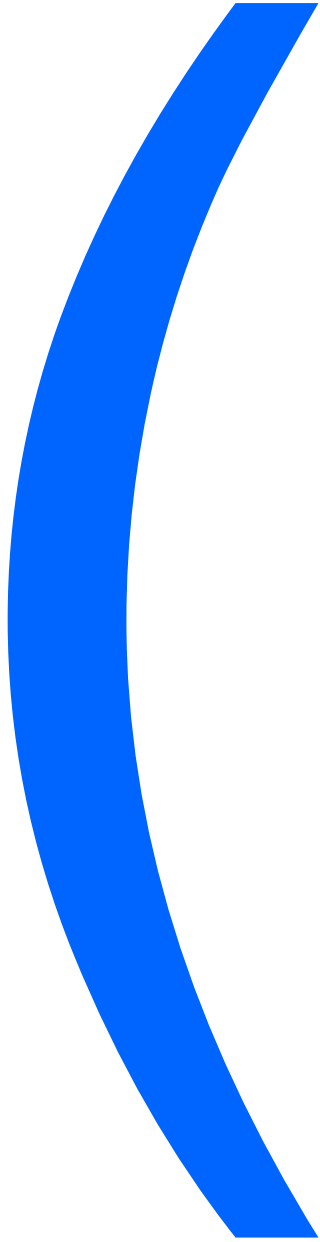
$$h_s = 3 \text{ kpc}$$

$$h_d = 3 \text{ kpc}$$

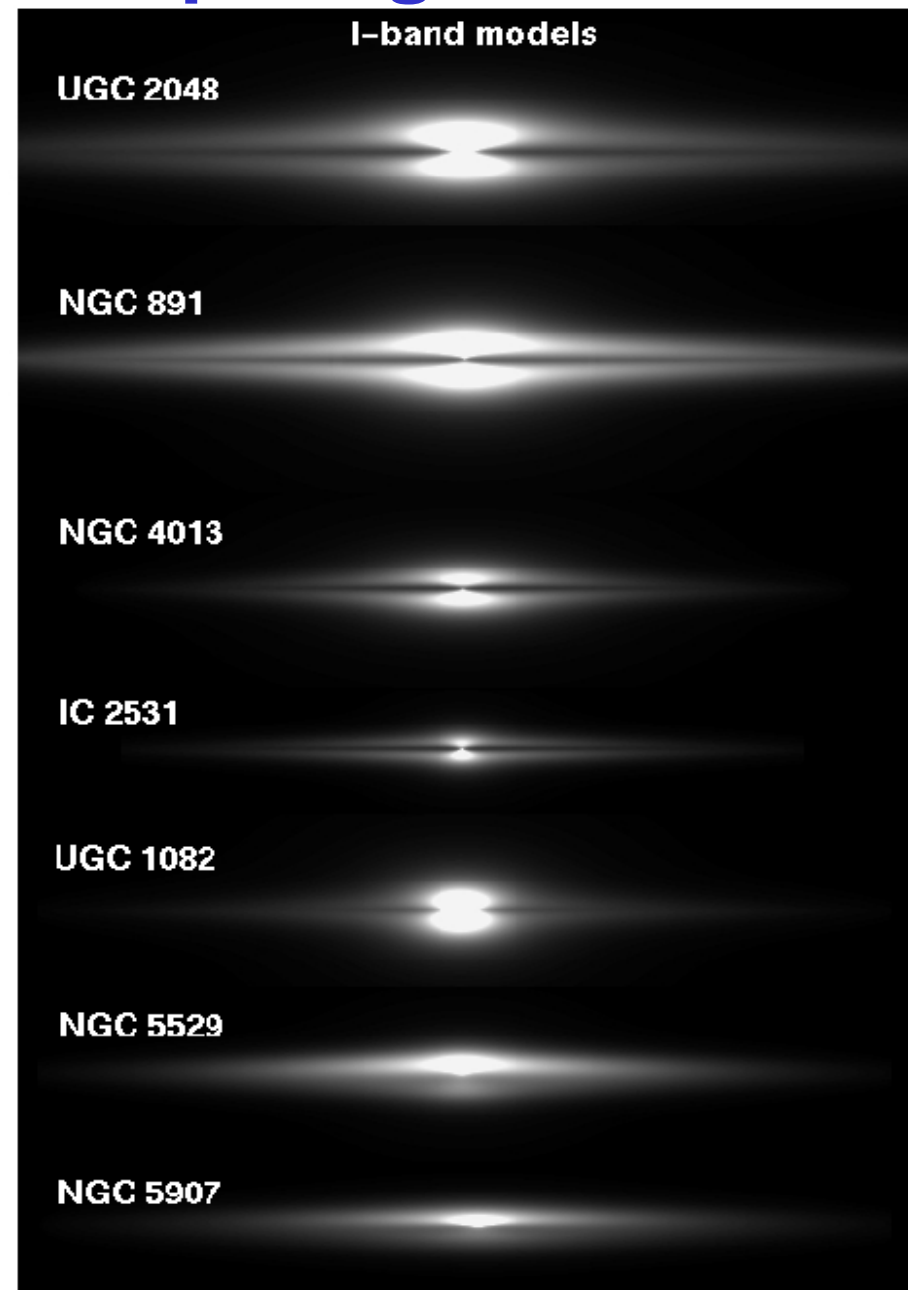
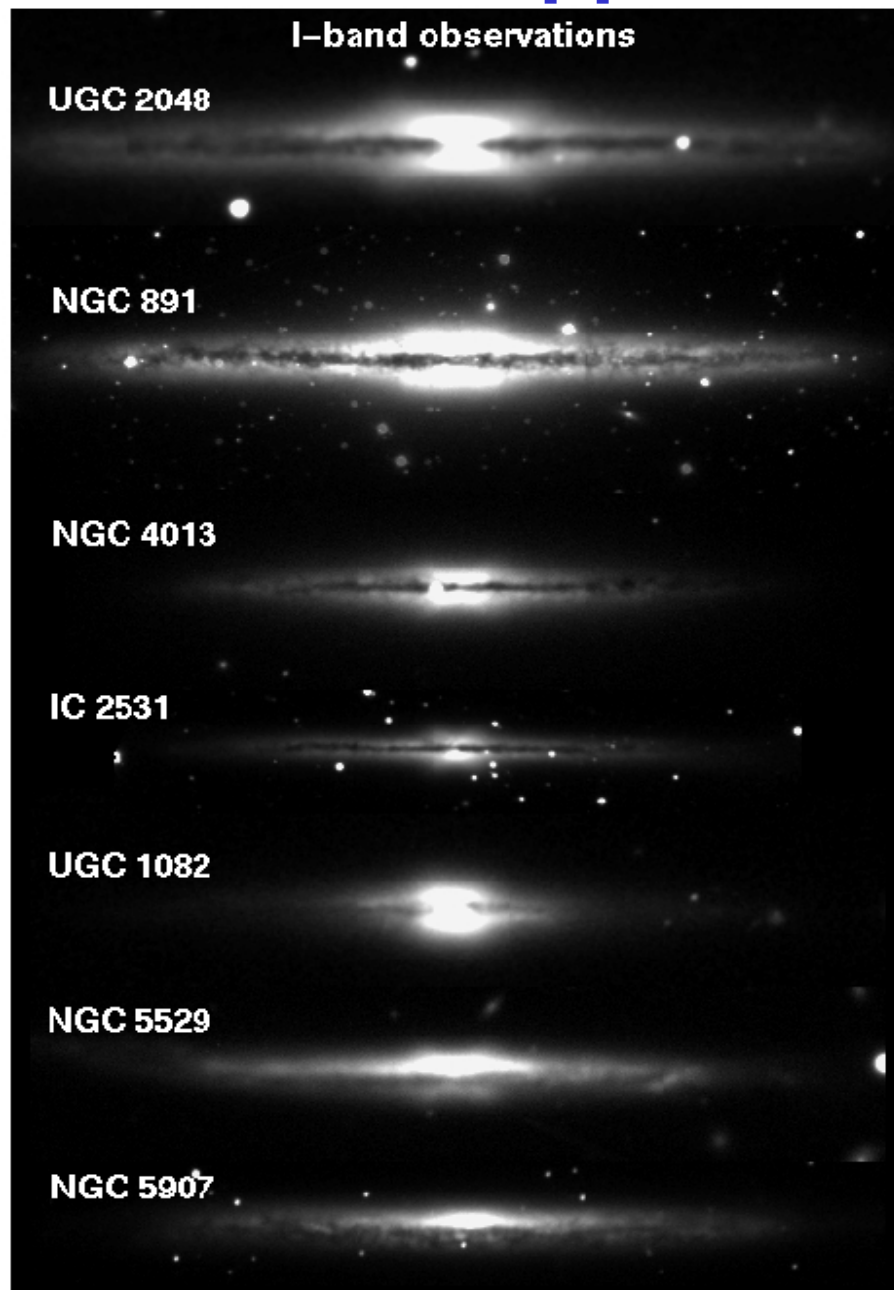
$$z_s = 0.3 \text{ kpc}$$

$$z_d = 0.15 \text{ kpc}$$



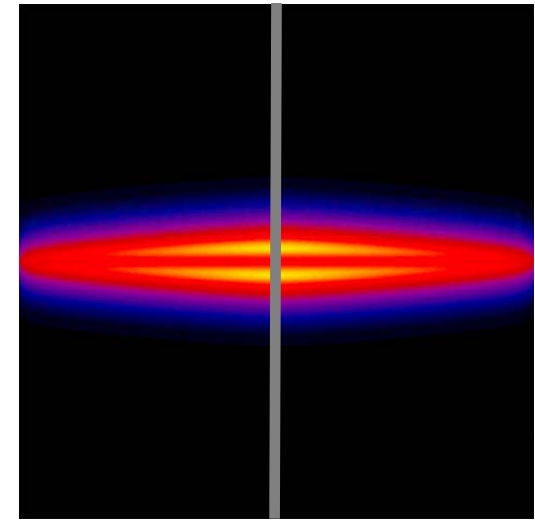
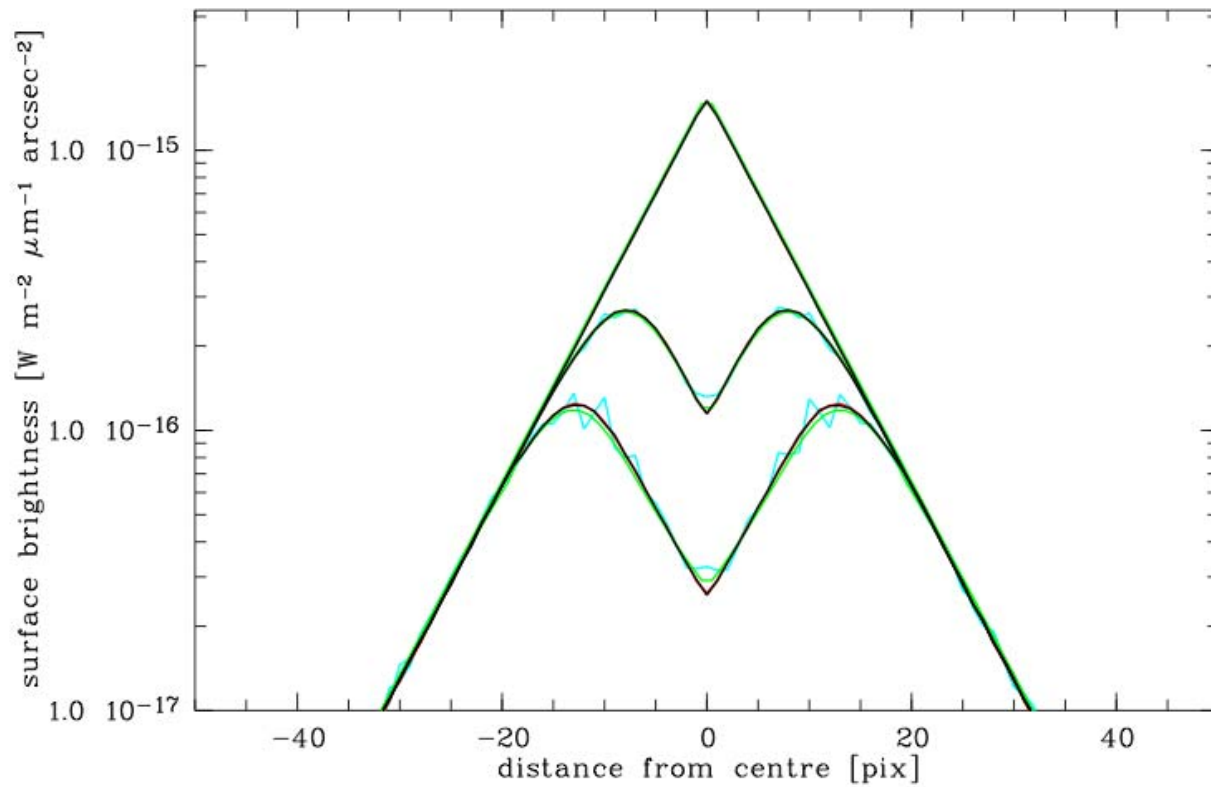


Model application in spiral galaxies



Xilouris et al, 1999, A&A, 344, 868

Code Comparison in galactic environments

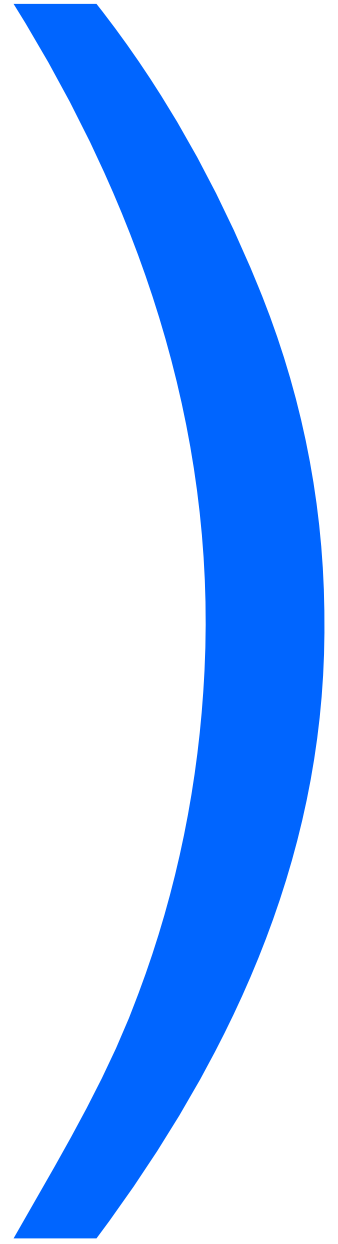


DIRTY – M.C.

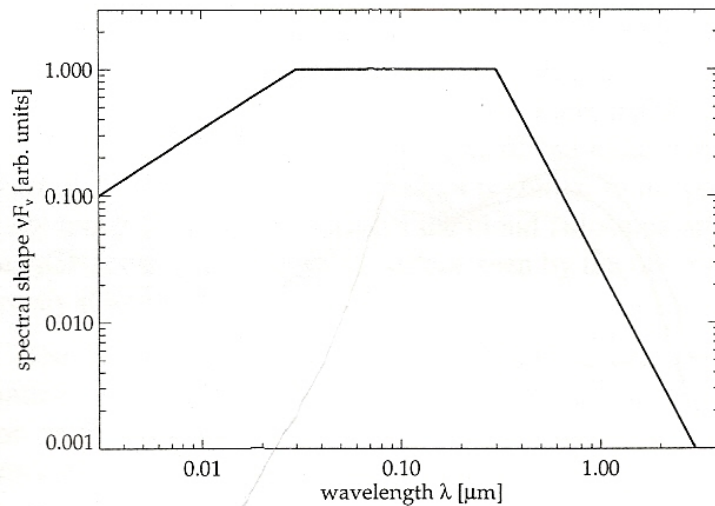
SKIRT – M.C.

TRADING – M.C.

CRETE – S.I.



SED of an accretion disk



Models with different inclination angle

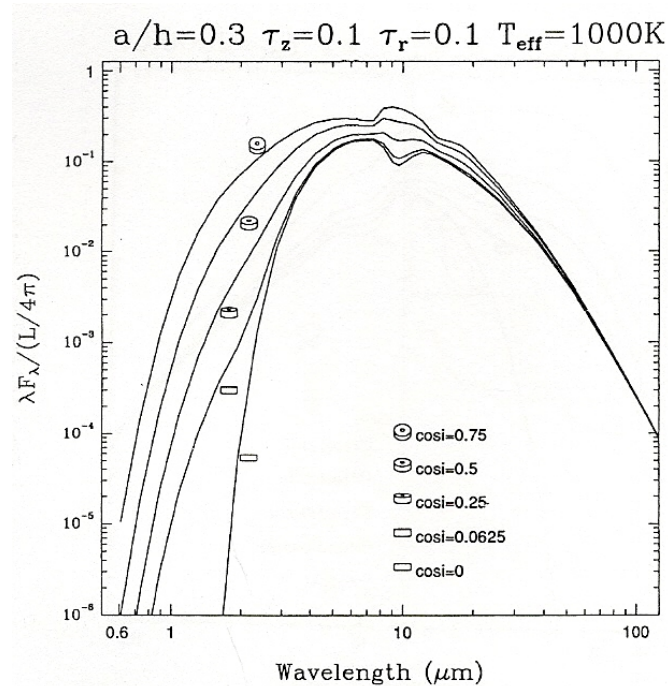
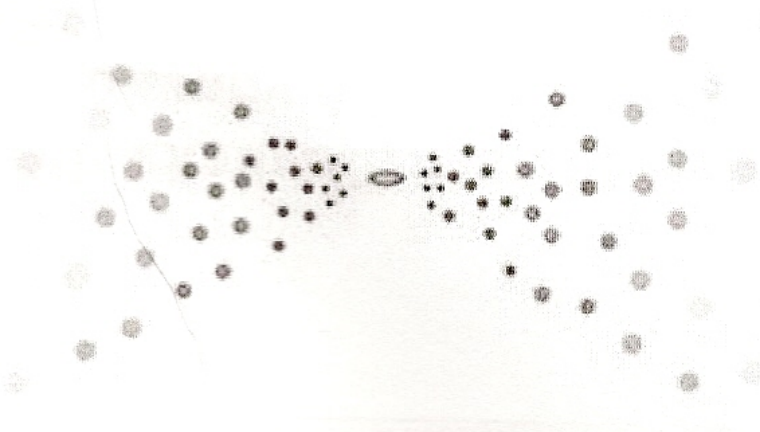


FIG. 5a

Clumpy geometry of a torus



Modeling the SED of NGC 1068

