

# PROCESSES CLOSE TO THE CENTRAL ENGINE OF AGN

Prof. K. Nandra  
Astrophysics Group  
Imperial College London

# OVERVIEW

- Theoretical Framework
  - 1.1 Radiative Processes
  - 1.2 Basic AGN properties
  - 1.3 Black hole accretion
  - 1.4 Relativistic effects
- Observations
  - 2.1 The X-ray continuum source
  - 2.2 The iron  $K\alpha$  line and Compton reflection
  - 2.3 Absorption
  - 2.4 The soft excess

# PART 1: THEORETICAL FRAMEWORK

# 1.1 RADIATIVE PROCESSES

- Blackbody Radiation
- Electron Scattering
- Line Emission and Absorption

# BLACKBODY RADIATION

**For matter and radiation in thermal equilibrium, radiation has the Planck spectrum:**

$$I(E) = \left( \frac{2}{h^2 c^2} \right) \left( \frac{E^3}{e^{E/k_B T} - 1} \right) d\nu$$

for  $E = h\nu \ll kT$  we have the Rayleigh - Jeans spectrum:

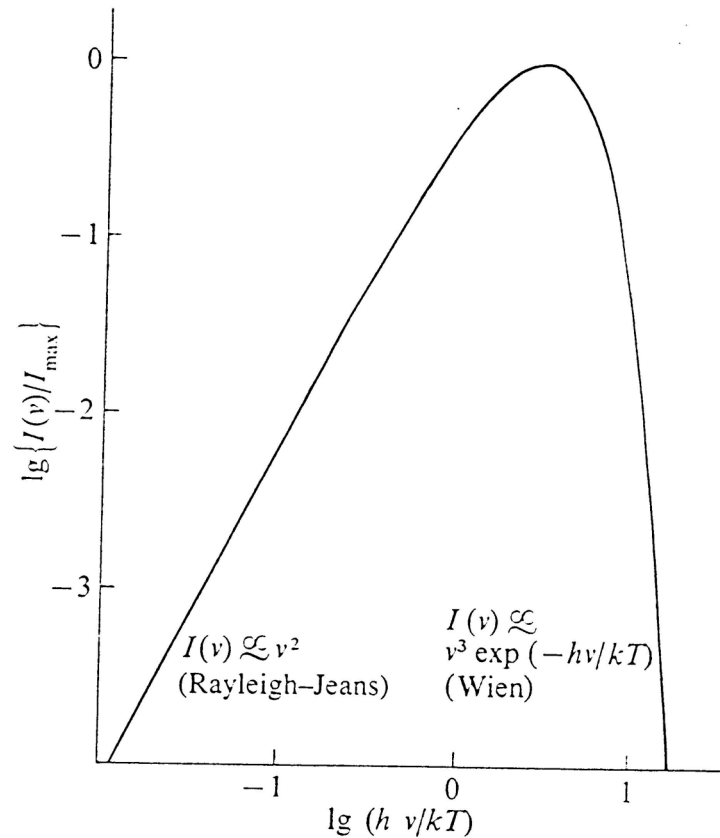
$$I(\nu) \propto \nu^2$$

for  $E = h\nu \gg kT$  we have the Wien spectrum:

$$I(\nu) \propto \nu^3 \exp(-h\nu/kT)$$

**Example in AGN physics: accretion disks**

# BLACKBODY EMISSION



Peak frequency :  $\nu_m = 2.821 \frac{k_B T}{h}$

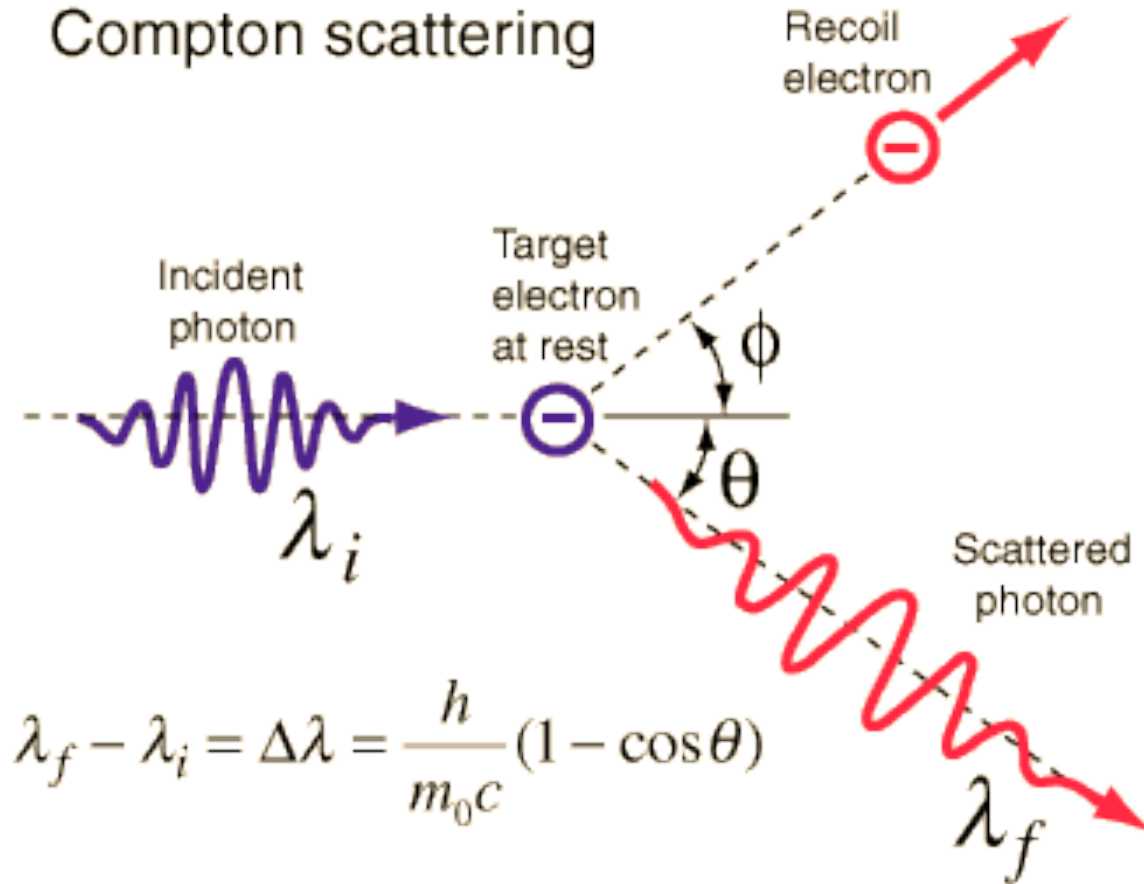
Energy density :

$$u_{\text{rad}} = \int_0^{\infty} \frac{4\pi}{c} I(\nu) d\nu = aT^4 \quad \text{where}$$

$$a = \left( \frac{8\pi^5 k_B^4}{15h^3 c^3} \right) = 7.565 \times 10^{-16} \text{ Jm}^{-3} \text{ K}^{-4}$$

**Fig. 1.9** The Planck blackbody spectrum. The intensity is given in units of the peak intensity.  $I_{\text{max}} = 1.9 \times 10^{-19} T^3 \text{ Wm}^{-2} \text{ sr}^{-1} \text{ Hz}^{-1}$ .

## Compton scattering



Thomson cross section:  $\sigma_T = 6.65 \times 10^{25} \text{ cm}^{-2}$

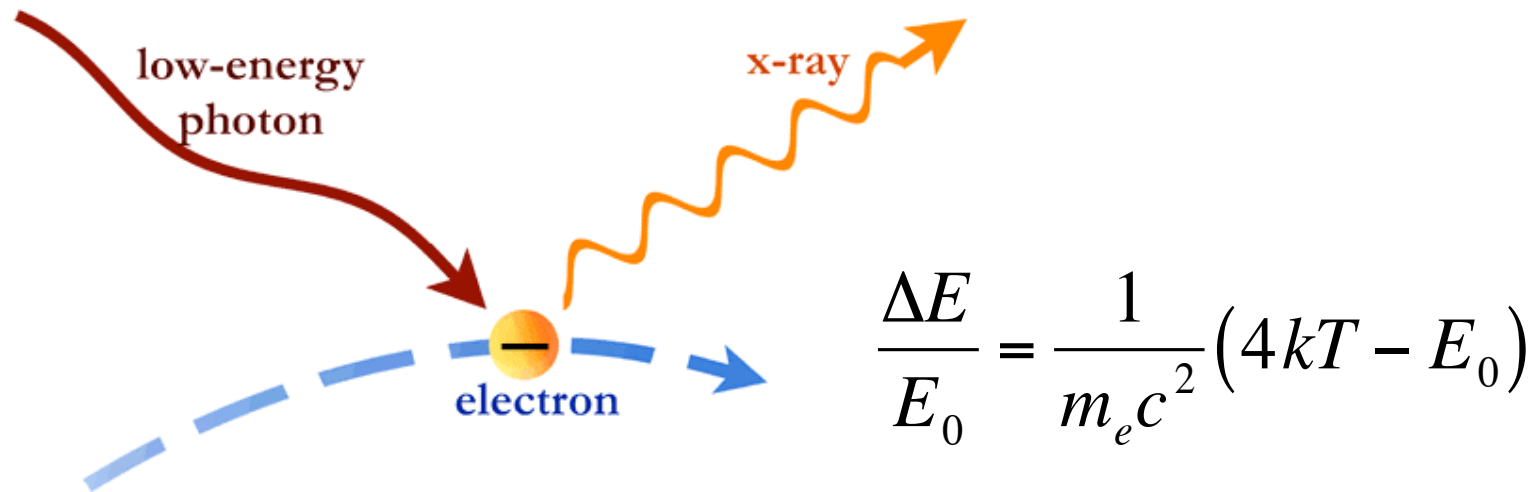
Thomson optical depth:  $\tau_T = \sigma_T N(H)$

“Optically thick”:  $\tau_T > 1$

## Example in AGN physics: reflection continuum

# INVERSE COMPTON EMISSION

- Photon  $E_0 = h\nu$  boosted in energy by hot  $e^-$  at  $kT$  to e.g. X-rays

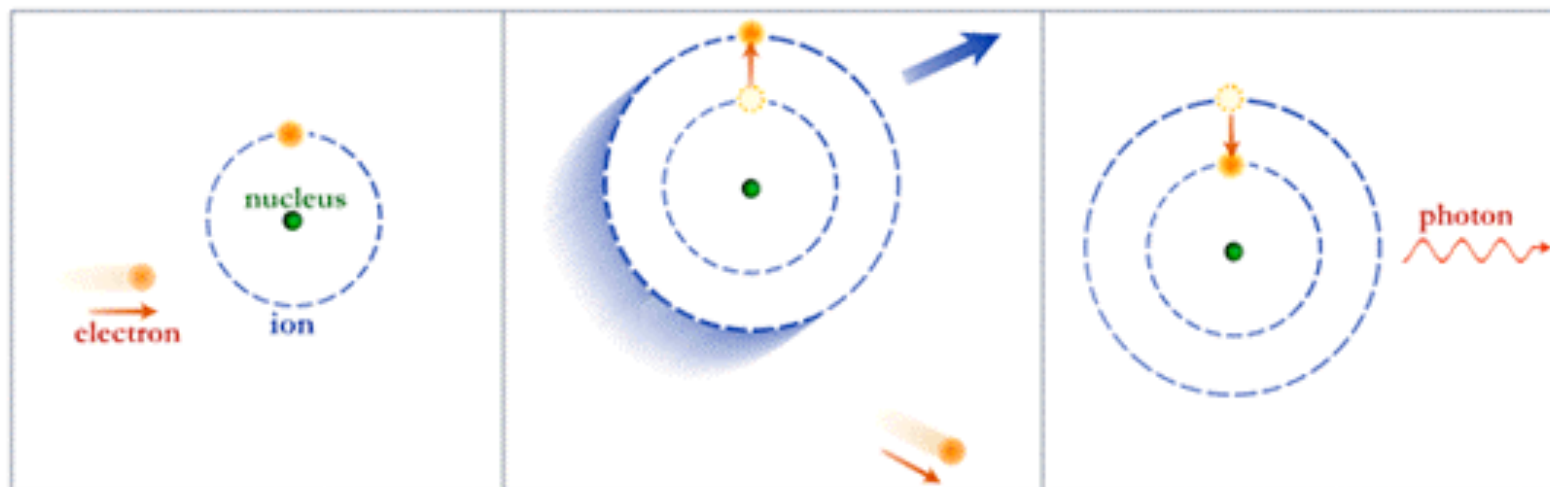


**Example in AGN physics: Primary X-ray continuum**



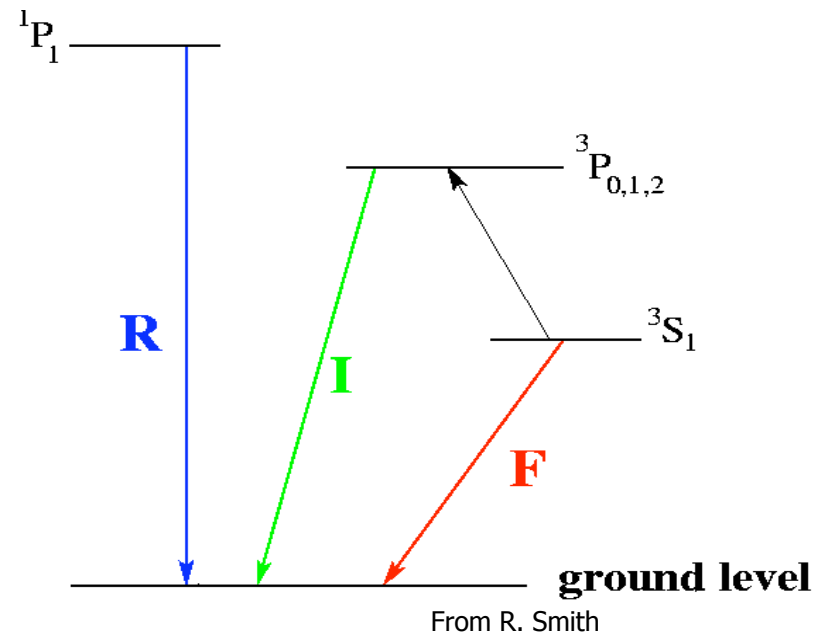
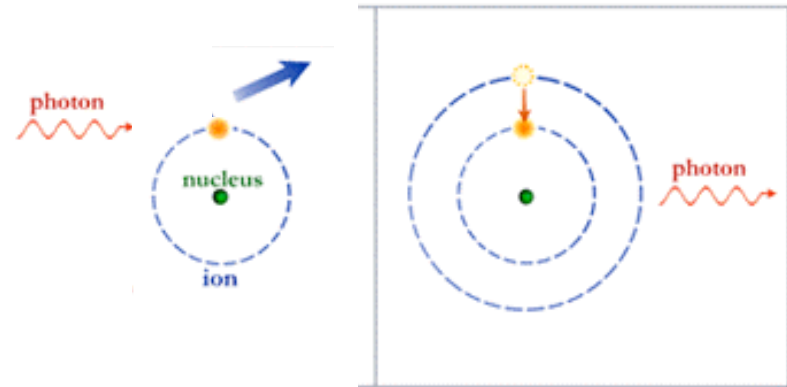
# LINE EMISSION

- Excitation of atoms by:
  - Thermal collisions
  - Radiative excitation
- Then radiative de-excitation



# TYPES OF LINE EMISSION

- Fluorescence:
  - Needs L-shell electrons
  - Photoionization, then either:
    - **2p->1s radiative transition**
    - *or* Auger ionization
    - **Fluorescence yield** measures ratio
- Recombination (ionized)
  - He and H-like are most important
  - Triplet: forbidden, resonance, intercombination



## STRONG X-RAY LINES (NEUTRAL)

Element	Transition	Energy (keV)
Carbon	C I $K\alpha_1$	0.277
Nitrogen	N I $K\alpha_1$	0.3924
Oxygen	O I $K\alpha_1$	0.525
Neon	Ne I $K\alpha_1, K\alpha_2$	0.849, 0.849
Magnesium	Mg I $K\alpha_1, K\alpha_2, K\beta_1$	1.253, 1.253, 1.302
Silicon	Si I $K\alpha_1, K\alpha_2, K\beta_1$	1.740, 1.740, 1.836
Sulphur	S I $K\alpha_1, K\alpha_2, K\beta_1$	2.308, 2.307, 2.464
<b>Iron</b>	<b>Fe I <math>K\alpha_1, K\alpha_2, K\beta_1</math></b>	<b>6.403, 6.391, 7.058</b>
	Fe I $L\alpha_1, L\alpha_2, L\beta_1$	0.705, 0.705, 0.719
Nickel	Ni I $K\alpha_1, K\alpha_2, K\beta_1$	7.478, 7.461, 8.265
	Ni I $L\alpha_1, L\alpha_2, L\beta_1$	0.852, 0.852, 0.869

From Bearden (1979)

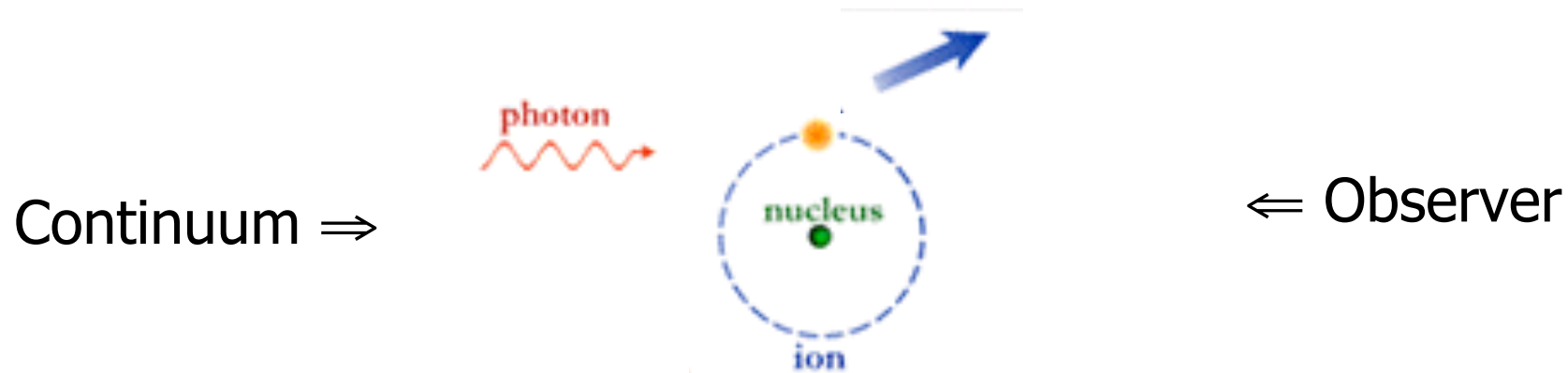
# STRONG X-RAY LINES (IONIZED)

<b>Element</b>	<b>Transition</b>	<b>Energy (keV)</b>
Nitrogen	N VII	0.3924
Oxygen	O VII O VIII	0.666, 0.698 0.816, 0.837, 0.846
<b>Iron</b>	<b>Fe XXVI</b> <b>Fe XXVI Ly<math>\alpha</math></b>	<b>6.63(f), 6.67(i), 6.70(r)</b> <b>6.89, 6.97</b>
Nickel	Ni XXVII Ni XXVIII L $\alpha$	7.75(f), 7.80(i), 7.80(r) 7.95

From XSTAR list (T. Kallman NASA/GSFC)

# PHOTOELECTRIC ABSORPTION

- Bound-free ionization of  $e^-$  by photon
- Threshold energy  $E_{th} = h\nu$  depending on ionization potential of atom (i.e. on  $Z$ )
- Abundant elements (C,N,O) are light: absorption dominant at soft ( $<1$  keV) X-rays



# PROMINENT X-RAY ABSORPTION EDGES

<b>Element</b>	<b>Transition</b>	<b>Energy (keV)</b>
Carbon	C I V, VI K	0.282, 0.392, 0.490
Nitrogen	N I, VI, VII K	0.397, 0.552, 0.667
Oxygen	O I, VII, VIII K	0.533, 0.739, 0.871
Neon	Ne I, IX, X K	0.876, 1.196, 1.362
Magnesium	Mg I, XI, XII K	1.309, 1.762, 1.963
Silicon	Si I, XIII, XIV K	1.840, 2.432, 2.673
Sulphur	S I, XV, XVI K	2.471, 3.214, 3.494
Iron	Fe I, XXV, XXVI K	7.112, 8.755, 9.278
	Fe I M2, L2, L3	0.538, 0.721, 0.707
Nickel	Ni I XXVII, XXVIII K	8.339, 10.19, 10.66

From T. Kallmann (GSFC) compilation

# PHOTOELECTRIC ABSORPTION

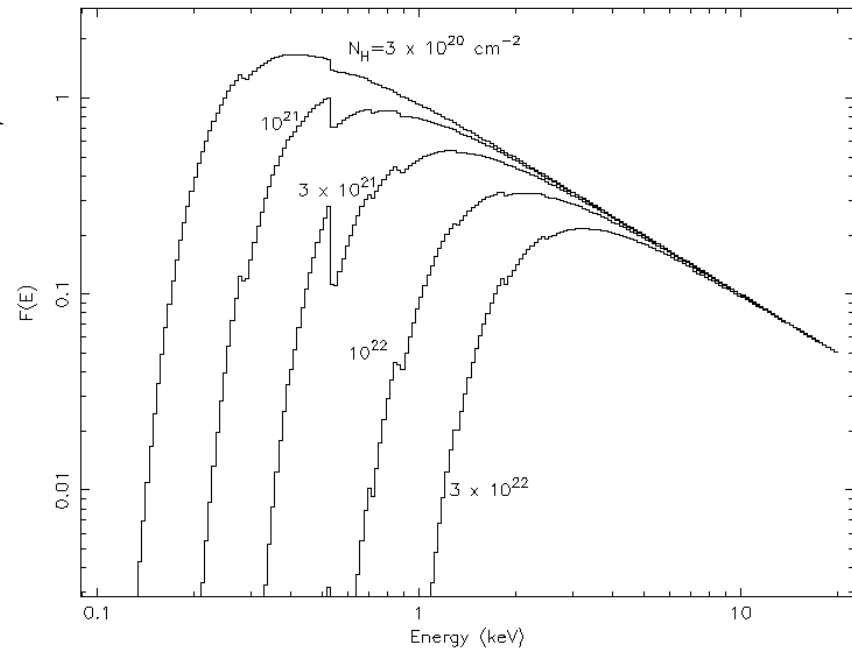
$N_H$  = Equivalent hydrogen column density ( $\text{cm}^{-2}$ )

$\sigma(E)$  = cross section ( $\text{cm}^2$ )

$\tau = \sigma(E)N_H$  = optical depth

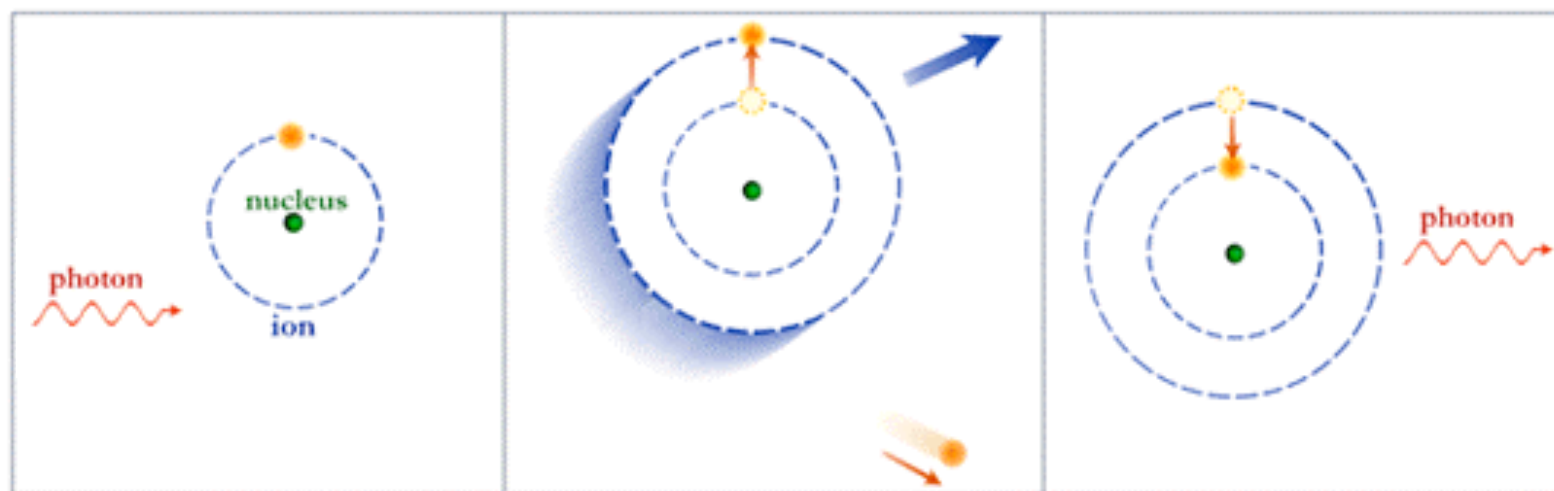
$F(E) = AE^{-\Gamma} e^{-\sigma(E)N_H}$

$\sigma(E) \approx E^{-3}$



Profile dominated by bound-free edges of abundant elements

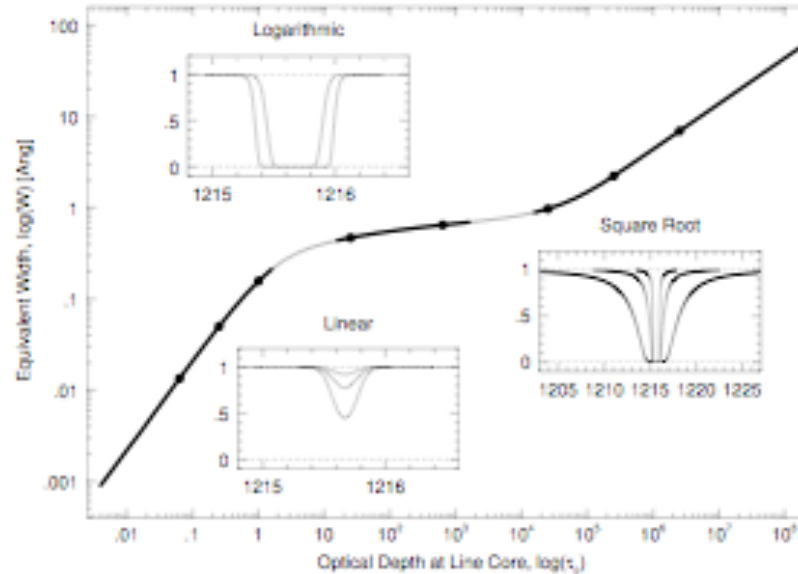
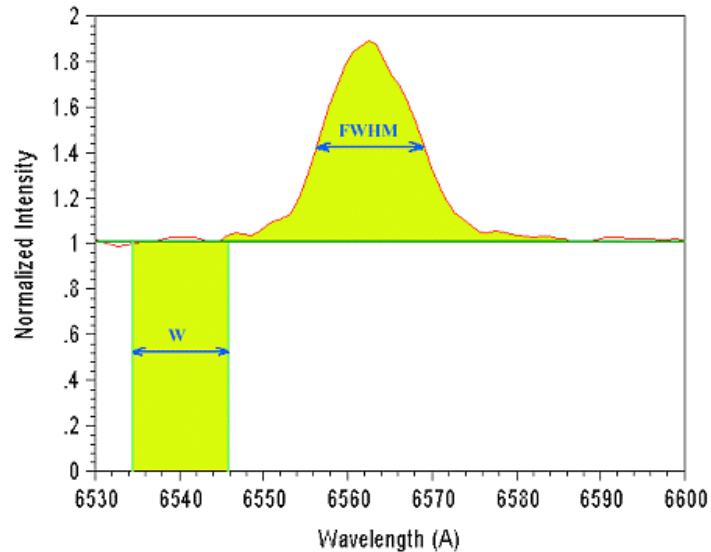
# ABSORPTION LINES



- Absorption by a specific transition in atom
- Cross-sections larger than photoelectric
- But only over a small wavelength range
- Strength depends on Doppler parameter  $b$
- Can measure  $N_{\text{H}}$ ,  $U$ , velocity etc.



# ABSORPTION LINES



Equivalent width:

$$EW = \frac{\int_{-\infty}^{\infty} F_l(E) dE}{F_c(E_l)}$$

$F_l$  = line flux,  $F_c$  = continuum flux,

$E_l$  = line energy

Curve of growth:

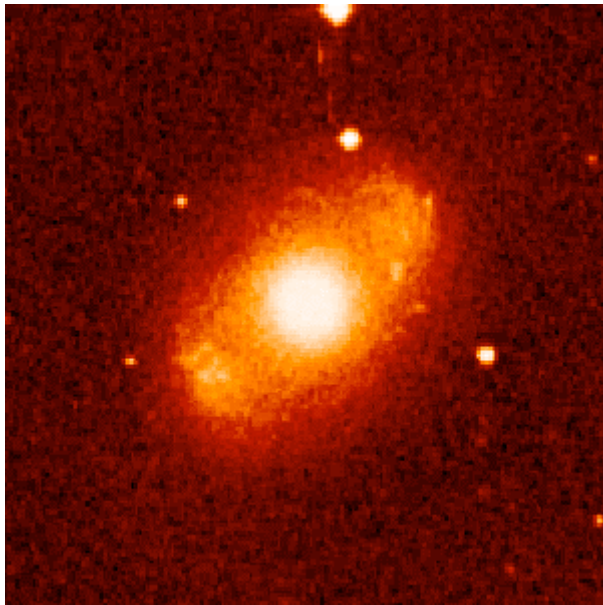
$\tau < 1$   $EW \propto N$  (linear)

$10 < \tau < 10^3$   $EW \approx const$  (saturated)

$\tau \gg 10^4$   $EW \propto \sqrt{N}$  (damping wings)

# 1.2 BASIC AGN PROPERTIES

ACTIVE: NGC 4151

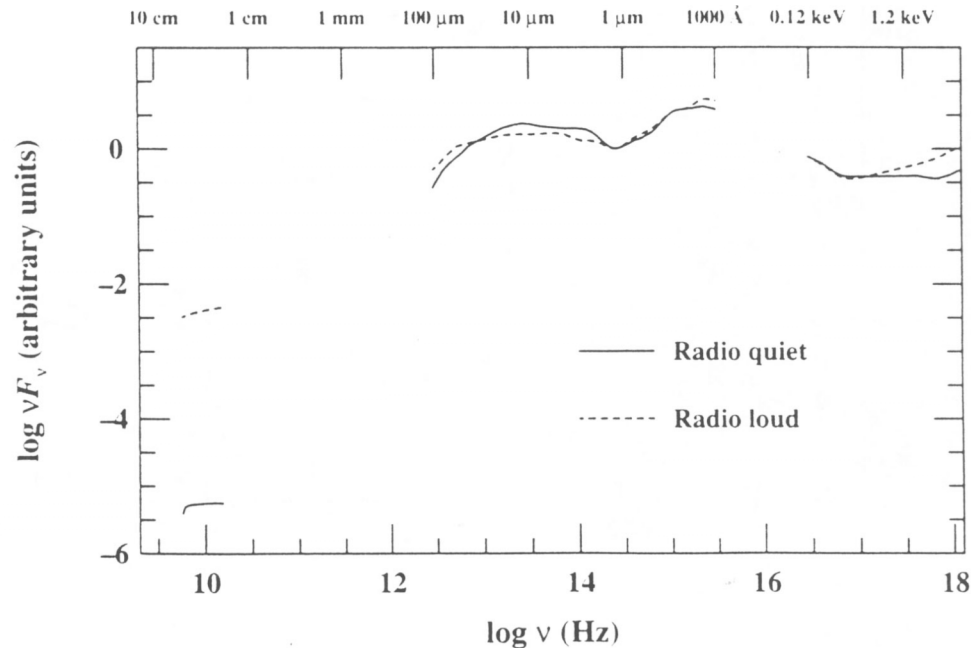


LINER: NGC 3031



# RADIATIVE PROPERTIES

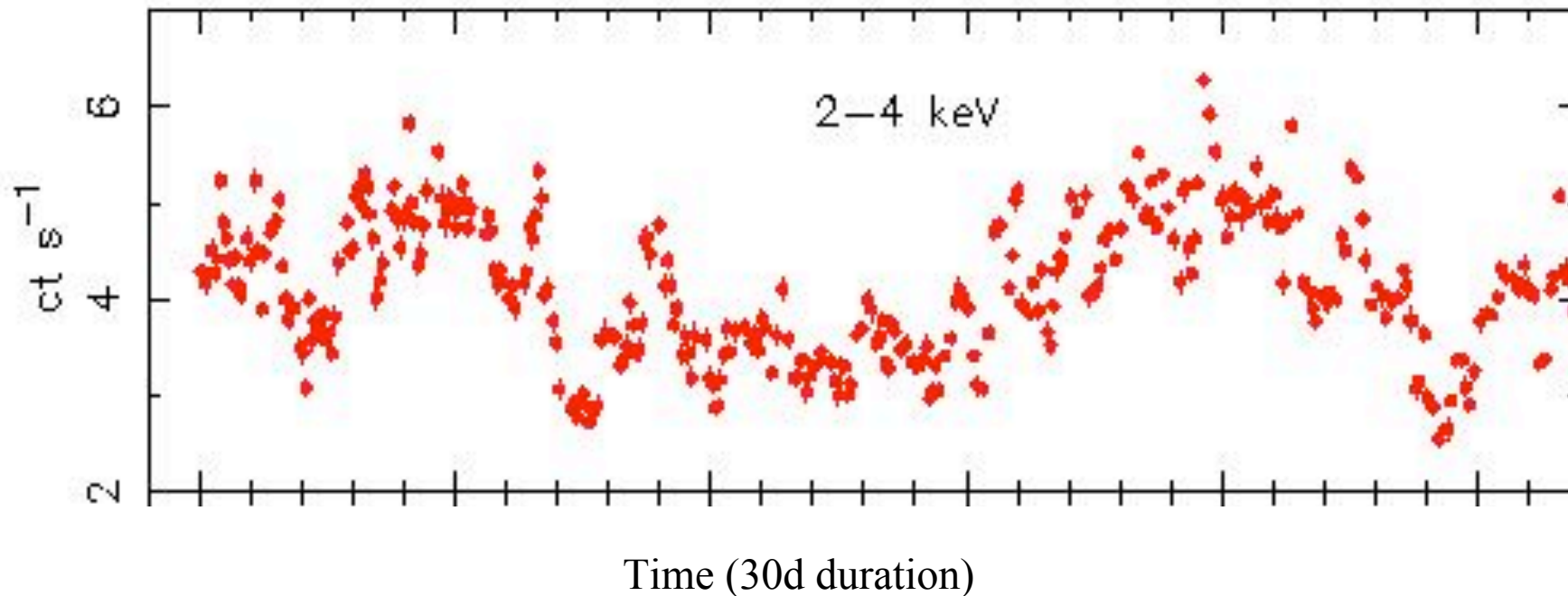
- AGN emit over a wide spectral range
- $L_{\text{bol}}$  can exceed  $10^{49}$  erg  $\text{s}^{-1}$
- ...or be as little as  $10^{39}$  (50% of galaxies?)
- Strongly variable, thus **compact** (L/R)



Spectral Energy Distribution (SED)

Elvis et al. 1994

# VARIABILITY



X-ray variability is the most extreme  
(NGC 7469 RXTE)

# X-RAY COMPACTNESS LEAGUE TABLE

	$L_x \text{ erg s}^{-1}$	R(cm)	$L_x/L_{\text{E}}^*$	R(AU)	L/R
AGN	$10^{40}\text{-}10^{47}$	$10^{14}\text{-}10^{16}$	$10^7\text{-}10^{14}$	2-200	$10^4\text{-}10^{13}$
Galaxy Clusters	$10^{43}\text{-}10^{46}$	$10^{24}\text{-}10^{26}$	$10^{10}\text{-}10^{13}$	$10^{10}\text{-}10^{12}$	$10^{-2}\text{-}10^3$
Normal Galaxies	$10^{38}\text{-}10^{40}$	$10^{22}\text{-}10^{23}$	$10^5\text{-}10^7$	$10^9\text{-}10^{10}$	$10^{-5}\text{-}10^{-2}$
Supernovae	$10^{35}\text{-}10^{37}$	$10^{17}\text{-}10^{19}$	$10\text{-}10^4$	$10^4\text{-}10^6$	$10^{-5}\text{-}1$
Stars, X-ray binaries	$10^{30}\text{-}10^{37}$	$10^6\text{-}10^{11}$	$10^{-3}\text{-}10^4$	$10^{-7}\text{-}10^{-2}$	$10^{-1}\text{-}10^{11}$

# EFFICIENCY ARGUMENT

(e.g. Fabian 1979; Brandt et al. 1998)

Outburst of accreted mass  $M$ , luminosity  $\Delta L$  in time  $\Delta t$

$$\Delta L \Delta t = \eta M c^2 \quad \eta = \text{radiative efficiency}$$

$$M \approx m_p n V \quad n = \text{number density, } V = \text{volume}$$

Source variability slowed down by scattering (photon diffusion):

$$\Delta t \geq (1 + \tau_T) \frac{R}{c} \quad \text{Thomson optical depth } \tau_T = n \sigma_T R$$

$$\text{Hence: } \eta \geq \frac{\Delta L}{\Delta t} f(\tau_T) \quad f(\tau_T) \propto \frac{(1 + \tau_T)^2}{\tau_T}$$

So  $\eta$  has a minimum value for a given  $\Delta L/\Delta t$  of:

$$\eta \geq 4.8 \times 10^{-43} \Delta L / \Delta t$$

AGN variations typically exceed  $\eta = 0.007$ , max for nuclear fusion

**→ ACCRETION POWERED SOURCES**

# BASIC PARAMETERS

Eddington limit:

$$F_{rad} = F_{grav}$$

$$L_{Edd} = \frac{4\pi GM \cdot m_p}{\sigma_T} = 1.26 \times 10^{38} \left( \frac{M}{M_\odot} \right) \text{ erg s}^{-1} \text{ (H only)}$$

$$= 1.52 \times 10^{38} \left( \frac{M}{M_\odot} \right) \text{ erg s}^{-1} \text{ (including He)}$$

Accretion Luminosity:

$$L = \eta \dot{M} c^2 \quad \dot{m} = \frac{L}{L_{Edd}} = \frac{\dot{M}}{\dot{M}_{Edd}}; \quad \dot{M}_{Edd} = \frac{L_{edd}}{\eta c^2}$$

efficiency depends on compact object (NS, BH, spinning BH)

# 1.3 BLACK HOLE ACCRETION

- Rapid variability: trillions of solar luminosities are generated in a region  $<10^{13-15}$  cm.
- Source is extremely compact and highly efficient – usually too efficient for stellar processes.
- Implied efficiency  $\eta > 0.1$  (10-100 x fusion)
- Eddington limit implies mass  $M > 8 \times 10^5 L_{44} M_{\odot}$
- Dynamical studies show masses of  $\sim 10^6 - 10^9 M_{\odot}$
- $\Rightarrow$  Compact object is a supermassive black hole



# DISK ACCRETION

- Accreting material will have angular momentum  $\Rightarrow$   
**ACCRETION DISK**

Accretion rate required to generate  $L = \eta \dot{m} c^2$

$$\dot{m} \approx 1.8 \times 10^{-3} L_{44} M_8 \text{ yr}^{-1}$$

Radial temperature profile

$$L \propto GM\dot{m} / R \propto 2\pi R^2 T^4 \quad (\text{local blackbody assumption})$$

Hence :

$$T(R) = M^{-0.25} \dot{m}^{0.25} R^{-0.75}$$

*Typical characteristic temperature is  $T_{bb} = 5 \cdot 10^5 M_8^{-0.25} K$*

# ALPHA DISKS

The classic solution for accretion disks was given by Shakura & Sunyaev (1973). SS disks can be either *gas pressure* or *radiation pressure* dominated.

Temperature, Flux and Density for Radiation dominated (small  $R$ ):

$$T = 3.1 \times 10^5 \alpha^{-1/4} M_8^{-1/4} \left( \frac{R}{R_g} \right)^{-3/8} K$$

$$F = 8.3 \times 10^{17} \left( \frac{R}{R_g} \right)^{-3} \left( \frac{\dot{M}}{M_{edd}} \right) M_8^{-1} \left( 1 - \left[ \frac{R_{in}}{R} \right]^{1/2} \right) \text{erg cm}^{-2} \text{s}^{-1}$$

$$n = 5.7 \times 10^{10} \alpha^{-1} \left( \frac{R}{R_g} \right)^{-3/2} \left( \frac{\dot{M}}{M_{edd}} \right)^{-2} M_8^{-1} \left( 1 - \left[ \frac{R_{in}}{R} \right]^{1/2} \right)^{-2}$$

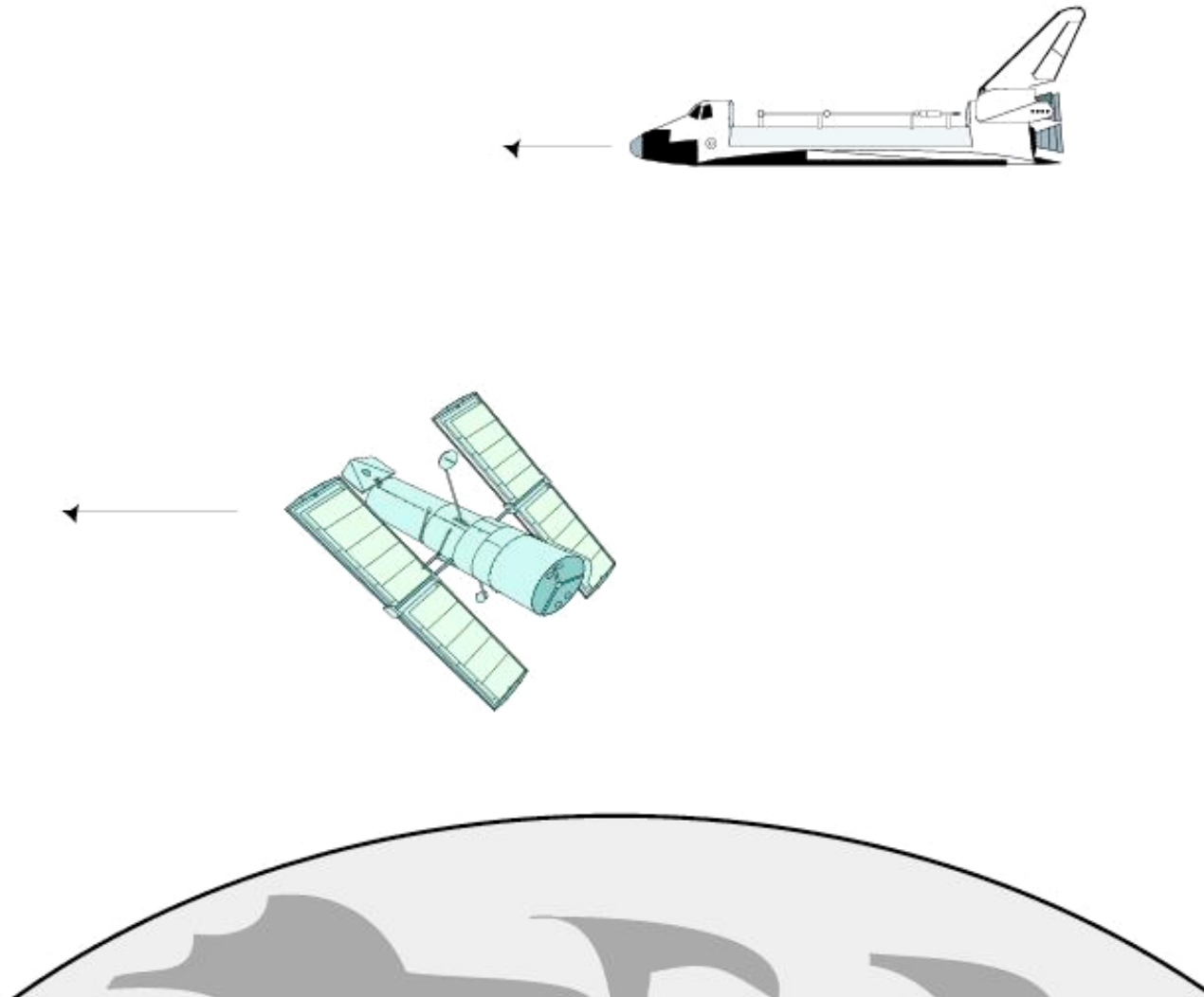
Viscosity parameter  $\alpha$  encompasses unknown physics!

# MAGNETO-ROTATIONAL INSTABILITY

- Disk threaded by weak magnetic field
- Radial fluid elements coupled by magnetic tension (like a spring)
- Outer element speeds up, moves out
- Inner element slows down, moves in – accretion happens!
- Provides angular momentum transport
- Unstable  $\Rightarrow$  turbulence

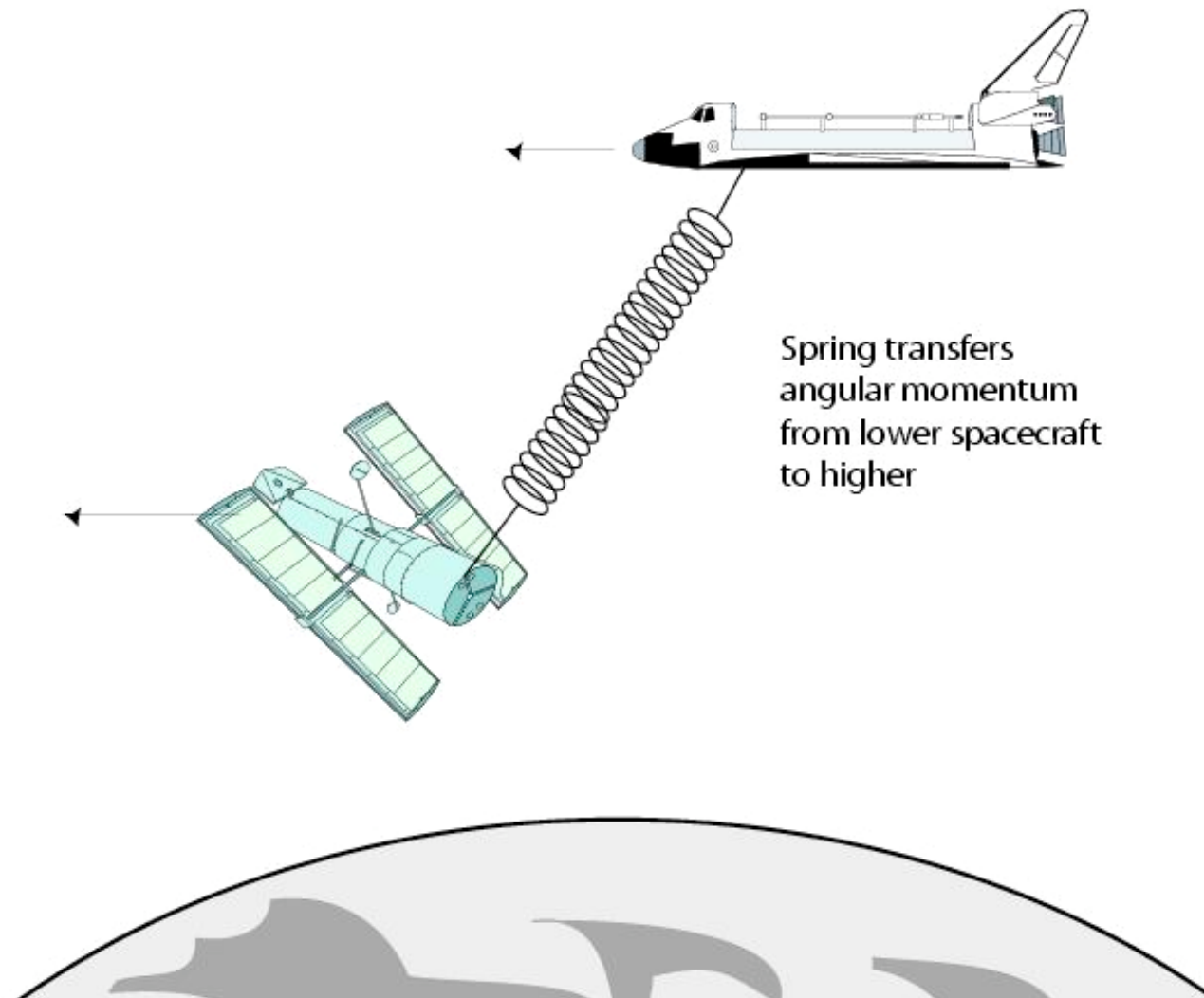
Orbital Dynamics  
Higher angular momentum = lower angular velocity

Slide: J. Hawley

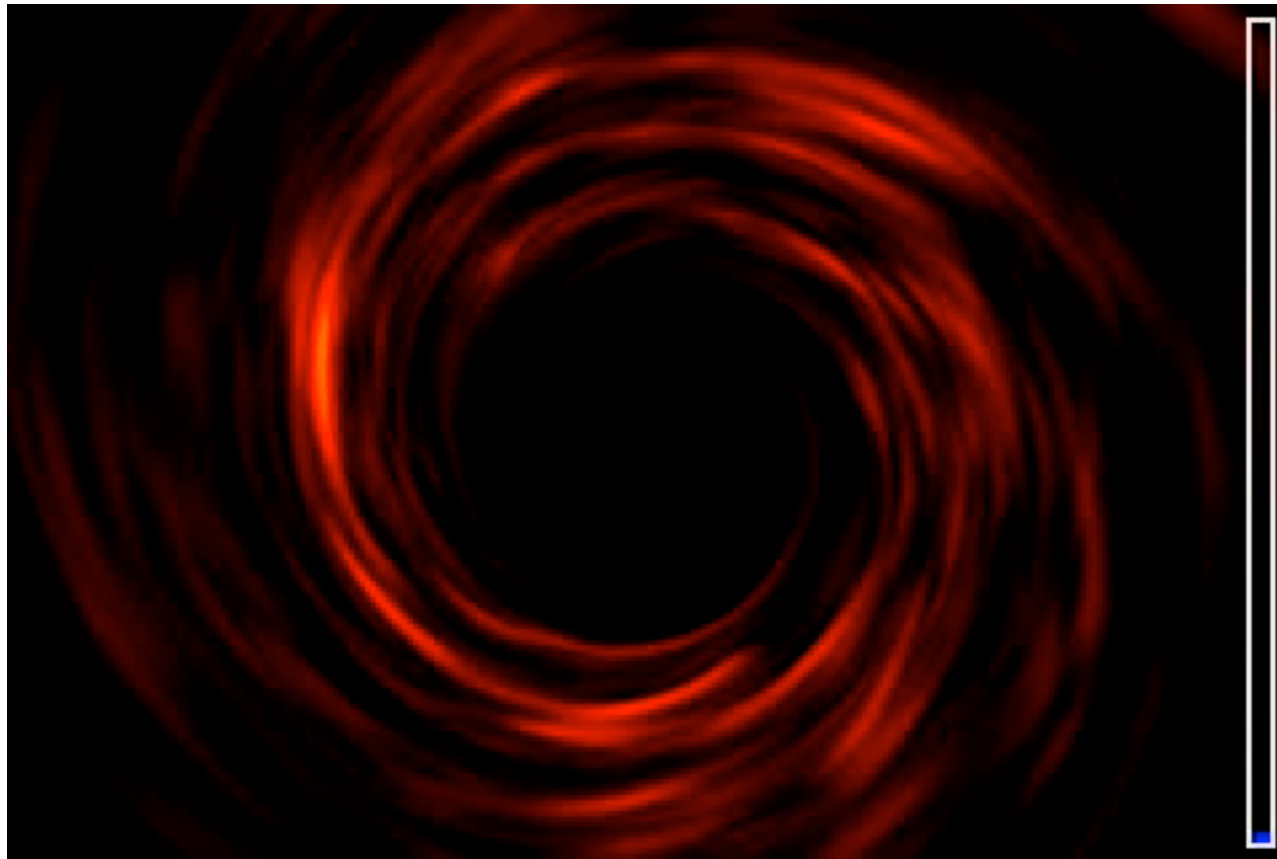


Orbital Dynamics  
Higher angular momentum = lower angular velocity

Slide: J. Hawley



# MHD SIMULATIONS



Armitage & Reynolds (2003)

# 1.4 RELATIVISTIC EFFECTS

- Black hole important at small radii
- Doppler shifts due to large velocities
- Gravitational redshift
- Time dilation
- Light bending/focussing

# BLACK HOLE FUNDAMENTALS

Schwarzschild Metric (non-rotating BH):

$$ds^2 = -\left(1 - \frac{R_s}{r}\right) c^2 dt^2 + \left(1 - \frac{R_s}{r}\right)^{-1} dr^2 + r^2 d\theta^2 + r^2 \sin^2 \theta d\phi^2$$

$$E_{obs} = E_{em} \sqrt{1 - \frac{2R_g}{R}} \quad (\text{Gravitational redshift})$$

$$R_s = 2R_g = \frac{2GM}{c^2} = 2.96 \times 10^{13} M_8 \text{ cm} \quad (\text{Schwarzschild radius})$$

$$R_{ms} = 6R_g \quad (\sim 20\% \text{ shift})$$

Infinite gravitational redshift at  $R=R_s$  (event horizon)

Kerr metric describes rotating black hole

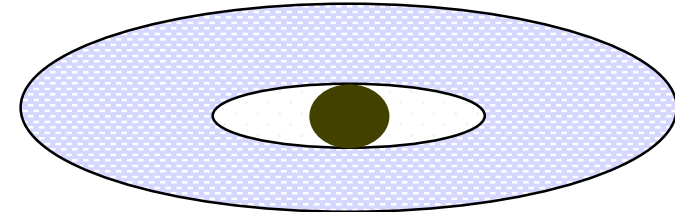
Event horizon at  $R \sim R_g$

Spin parameter  $a/M=0-1$   
Schwarzschild  $\rightarrow$  Maximal Kerr

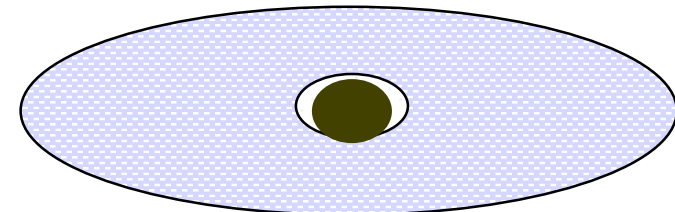


# THE ISCO

- Stable orbits cannot exist arbitrarily close to the BH
- Radius of marginal stability  $r_{ms}$  or Innermost Stable Circular Orbit (ISCO)
- Depends on black hole spin:



*SCHWARZSCHILD = NON-ROTATING*



*KERR = ROTATING*

Schwarzschild ( $a=0$ ):  $r_{ms} = 6 r_g$

Maximal Kerr ( $a \sim 1$ ) prograde:  $r_{ms} \sim r_g$

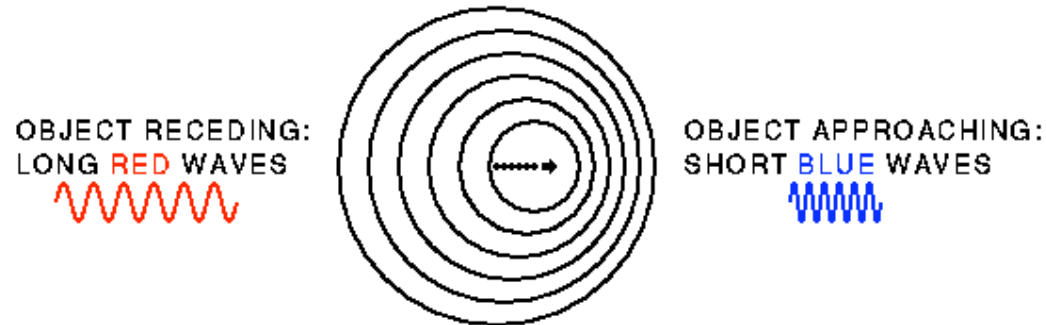
Maximal Kerr ( $a \sim 1$ ) retrograde:  $r_{ms} \sim 9 r_g$

Measuring ISCO can constrain spin\*\*

*\*\*But emission within  $r_{ms}$  possible for Schwarzschild (Reynolds & Begelman 1997)*

# ENERGY SHIFTS

$$z = \frac{\Delta\nu}{\nu_0} = \frac{\nu_e - \nu_0}{\nu_0} \approx \frac{v}{c} \quad \text{for } v \ll c \quad (\text{Classical Doppler})$$



$$z = 1 - \sqrt{\frac{1 + v/c}{1 - v/c}} \quad (\text{SR: } v \approx c + \text{ beaming/aberration})$$

$$E_{obs} = E_{em} \sqrt{1 - \frac{2R_g}{R}} \quad (\text{gravitational redshift})$$

$$R_g = \frac{GM}{c^2} = 1.48 \times 10^{13} M_8 \text{ cm}$$

$$R_{ms} = 6R_g \quad (\sim 20\% \text{ shift})$$

# LINES FROM A RELATIVISTIC DISK

